



# education

Department of  
Education  
FREE STATE PROVINCE

## PREPARATORY EXAMINATION *VOORBEREIDENDE EKSAMEN*

**GRADE/GRAAD 12**

**MATHEMATICS P1/WISKUNDE V1**

**SEPTEMBER 2020**

**MARKS/PUNTE: 150**

**MARKING GUIDELINES/NASIENRIGLYNE**

These marking guidelines consists of 19 pages.  
*Hierdie nasienriglyne bestaan uit 19 bladsye.*

**NOTE:**

- If a candidate answered a question TWICE, mark only the FIRST attempt.
- If a candidate has crossed out an attempt to answer a question and did not redo it, mark the crossed-out version.
- Consistent accuracy applies in ALL aspects of the marking guidelines.
- Stop marking at the second mistake related to a mark.
- Assuming answers/values in order to solve a problem is NOT acceptable.

**LET WEL:**

- *Indien 'n kandidaat 'n vraag TWEE keer beantwoord het, merk slegs die EERSTE poging.*
- *As 'n kandidaat 'n poging om 'n vraag te beantwoord, doodgetrek het en nie oorgedoen het nie, sien die doodgetrekte poging na.*
- *Volgehoue akkuraatheid is op ALLE aspekte van die nasienriglyne van toepassing.*
- *Staak nasien by die tweede fout geassosieer met 'n punt.*
- *Die veronderstelling van antwoorde/waardes in probleemoplossing, word NIE toegelaat NIE.*

<b>1</b>	<b>QUESTION 1/VRAAG 1</b>	
1.1		
1.1.1	$(x+5)(x-3) = -15$ $x^2 + 2x - 15 + 15 = 0$ $x^2 + 2x = 0$ $x(x+2) = 0$ $x = 0 \quad \text{OR/OF} \quad x = -2$	✓ standard form/ standaardvorm  ✓ factors/faktore  ✓ BOTH answers/BEIDE antwoorde  (3)
1.1.2	$3x^2 - 4x - 11 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(3)(-11)}}{2(3)}$ $x = \frac{4 \pm \sqrt{148}}{6}$ $x = 2,69 \quad \text{OR/OF} \quad x = -1,36$	✓ correct substitution into correct formula/korrekte substitusie in korrekte formule  ✓ simplification/ vereenvoudiging  ✓✓ answers/antwoorde  <b>-1 for rounding only once/-1 vir afronding slegs een maal</b> (4)
1.1.3	$2x^2 - 3 \geq 5x$ $2x^2 - 5x - 3 \geq 0$ $(2x+1)(x-3) \geq 0$ $x \leq -\frac{1}{2} \quad \text{OR/OF} \quad x \geq 3$ <p><b>ALTERNATIVE/ALTERNATIEWE</b></p> $x \in (-\infty; -\frac{1}{2}] \quad \text{OR/OF} \quad x \in [3; \infty)$	✓ standard form/standaardvorm  ✓ factors/faktore  ✓✓ answer/antwoorde  <b>Last 2 marks combo/Laaste 2-puntkombinasie</b> <b>If AND max 2/4/As EN maks 2/4</b> <b>If; max 2/4/As; maks 2/4</b> <b>Wrong notation max 2/4/ Verkeerde notasie maks 2/4</b>  (4)

<p>1.1.4</p> $\sqrt{2x+1} + 1 + \frac{12}{\sqrt{2x+1} + 3} = 5$ <p>Let <math>k = \sqrt{2x+1}</math> then</p> $k + 1 + \frac{12}{k + 3} = 5$ $k^2 + 4k + 3 + 12 = 5k + 15$ $k^2 - k = 0$ $k(k - 1) = 0$ $\sqrt{2x+1} = 0 \quad \text{OR/OF} \quad \sqrt{2x+1} = 1$ $2x+1=0 \quad \text{OR/OF} \quad 2x+1=1$ $x = -\frac{1}{2} \quad \text{OR/OF} \quad x = 0$ <p>Both answers applicable/beide antwoorde korrek</p>	<ul style="list-style-type: none"> <li>✓ <math>k = \sqrt{2x+1}</math></li> <li>✓ x LCM/x KGV</li> <li>✓ standard form/standaardvorm</li> <li>✓ factors or formula/faktore of formule</li> <li>✓ answers WITH CHOICE/antwoorde MET KEUSE</li> </ul> <p>(5)</p>
<p><b>ALTERNATIVE/ALTERNATIEWE</b></p> $\sqrt{2x+1} + 1 + \frac{12}{\sqrt{2x+1} + 3} = 5$ $2x+1+3\sqrt{2x+1}+\sqrt{2x+1}+3+12=5\sqrt{2x+1}+15$ $2x+1=\sqrt{2x+1}$ $4x^2 + 4x + 1 = 2x + 1$ $4x^2 + 2x = 0$ $2x(2x + 1) = 0$ $x = -\frac{1}{2} \quad \text{OR/OF} \quad x = 0$	<ul style="list-style-type: none"> <li>✓ x LCM/x KGV</li> <li>✓ squaring both sides/kwadreer weerskante</li> <li>✓ standard form/standaardvorm</li> <li>✓ factors or formula/faktore of formule</li> <li>✓ answers WITH CHOICE/antwoorde MET KEUSE</li> </ul>



<p>1.1.5</p> $\sqrt[3]{x^2} - 4\sqrt[3]{x} - 5 = 0$ $x^{\frac{2}{3}} - 4x^{\frac{1}{3}} - 5 = 0$ $\left( x^{\frac{1}{3}} - 5 \right) \left( x^{\frac{1}{3}} + 1 \right) = 0$ $x^{\frac{1}{3}} = 5 \quad \text{OR/OF} \quad x^{\frac{1}{3}} = -1$ $x = 125 \quad \text{OR/OF} \quad x = -1$	<ul style="list-style-type: none"> <li>✓ simplify/vereenvoudig</li> <li>✓ factors/faktore</li> <li>✓ equations/vergelykings</li> <li>✓ both answers/beide antwoorde</li> </ul> <p>(4)</p>
<p>1.2</p> $2x^3 - 3x^2 - 17x - 12 = (x+1)(x-4)(2x+3) \text{ given}$ $\therefore 2(y-2)^3 - 3(y-2)^2 + 17(2-y) = 12$ <p>Let <math>k = y - 2</math></p> $\therefore 2k^3 - 3k^2 - 17k - 12 = 0$ $(k+1)(k-4)(2k+3) = 0$ $k = -1 \quad \text{OR/OF} \quad k = 4 \quad \text{OR/OF} \quad 2k = -3$ $\therefore y - 2 = -1 \quad \text{OR/OF} \quad y - 2 = 4 \quad \text{OR/OF}$ $2y - 4 = -3$ $y = 1; y = 6; y = \frac{1}{2}$	<ul style="list-style-type: none"> <li>✓ method/metode</li> <li>✓ 1</li> <li>✓ 6</li> <li>✓ <math>\frac{1}{2}</math></li> </ul> <p>(4)</p>
<p><b>ALTERNATIVE/ALTERNATIEWE</b></p> $(y-2+1)(y-2-4)(2(y-2)+3) = 0$ $y = 1; y = 6; y = \frac{1}{2}$ <p><b>ALTERNATIVE/ALTERNATIEWE</b></p> $2y^3 - 15y^2 + 19y - 6 = 0$ $(y-1)(y-6)(2y-1) = 0$ $y = 1; y = 6; y = \frac{1}{2}$	<p>Using factor and remainder theorem/ Gebruik res- en faktorstelling</p>
	[24]

<b>QUESTION 2/VRAAG 2</b>	
2.1	<p>Quadratic sequence/Kwadratiese ry</p> <p><math>1; x; 1; -2; y; \dots; -322</math></p>
2.1.1	<p><math>1 \quad x \quad 1 \quad -2 \quad y</math></p> <p><math>x - 1; 1 - x; -3; y + 2 \quad 1^{\text{st}} \text{ diff}</math></p> <p><math>-2x + 2; x - 4; y + 5 \quad 2^{\text{nd}} \text{ diff}</math></p> <p><math>\therefore -2x + 2 = x - 4</math></p> <p><math>3x = 6</math></p> <p><math>x = 2 \quad \mathbf{AND/EN} \quad x - 4 = y + 5</math></p> <p><math>\therefore 2 - 4 = y + 5</math></p> <p><math>y = -7</math></p> <p style="text-align: right;">(4)</p>
2.1.2	<p>Hence quadratic sequence/Vervolgens</p> <p><math>1; 2; 1; -2; -7; \dots</math></p> <p><math>1; -1; -3; -5 \quad \text{first difference}</math></p> <p><math>-2; -2; -2 \quad \text{second difference}</math></p> <p><math>2a = -2 \quad 3a + b = 1 \quad a + b + c = 1</math></p> <p><math>a = -1 \quad b = 4 \quad c = -2</math></p> <p><math>\therefore -n^2 + 4n - 2 = -322</math></p> <p><math>n^2 - 4n - 320 = 0</math></p> <p><math>(n - 20)(n + 16) = 0 \quad \text{or formula/of formule}</math></p> <p><math>n = 20 \quad \mathbf{OR/OF} \quad n = -16</math></p> <p><math>\therefore 20 \text{ terms}/20 \text{ terme}</math></p> <p style="text-align: right;">(5)</p>

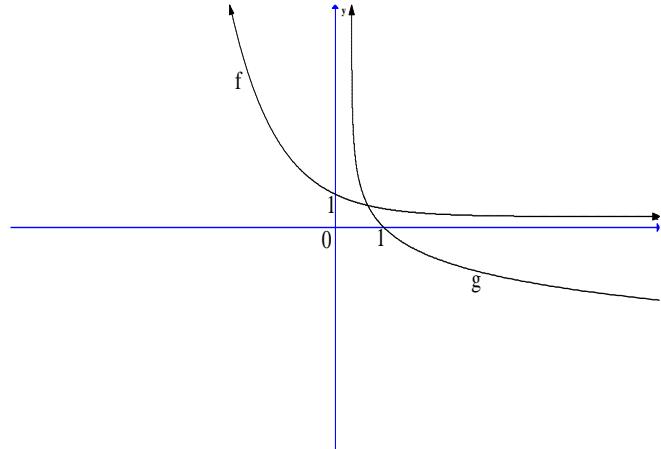
2.2	$S_n = 5n - 3$ $\therefore T_{34} = S_{34} - S_{33}$ $= 5(34) - 3 - [5(33) - 3]$ $= 5$	✓ formula/formule ✓ substitution/substitusie ✓ answer/antwoord  (3)
2.3	$a + 9d = 28$ equation 1/ vergelyking 1 $a + 4d + a + 6d = 32$ $2a + 10d = 32$ $a + 5d = 16$ equation 2/ vergelyking 2 equation 1 – equation 2: $4d = 12$ $d = 3 \quad \therefore a = 1$ $S_{50} = \frac{50}{2} [2(1) + (50 - 1)3]$ $= 3725$	✓ formula $T_{10}$ /formule $T_n$ ✓ formula $T_5 + T_7$ /formule $T_5 + T_7$ ✓ BOTH $a$ and $d$ /BEIDE $a$ en $d$ ✓ correct substitution in correct formula/korrekte substitusie in korrekte formule ✓ answer/antwoord  (5)
		[17]
	<b>QUESTION 3/VRAAG 3</b>	
3.1	$S_n = a + ar + ar^2 + \dots + ar^{n-1}$ $rS_n = ar + ar^2 + \dots + ar^{n-1} + ar^n$ $\therefore S_n - rS_n = a - ar^n$ $S_n(1 - r) = a(1 - r^n)$ $S_n = \frac{a(1 - r^n)}{1 - r}$	✓ expand $S_n$ /brei uit ✓ expand $rS_n$ /brei uit ✓ subtract/trek af ✓ common factor/gemene faktor  (4)

<p>3.2 Geometric sequence/<i>Meetkundige ry</i></p> <p><math>\sqrt{3}; \sqrt{3}-1; \dots</math></p> $r = \frac{\sqrt{3}-1}{\sqrt{3}} = \frac{\sqrt{3}(\sqrt{3}-1)}{\sqrt{3}\sqrt{3}} = \frac{3-\sqrt{3}}{3}$ <p><math>a = \sqrt{3}</math></p> $S_{\infty} = \frac{a}{1-r}$ $S_{\infty} = \frac{\sqrt{3}}{1 - \frac{3-\sqrt{3}}{3}} = \frac{\sqrt{3}}{\frac{3-(3-\sqrt{3})}{3}} = \sqrt{3} \times \frac{3}{\sqrt{3}}$ $= 3$	<ul style="list-style-type: none"> <li>✓ value of <math>r</math>/<i>waarde van r</i></li> <li>✓ correct substitution in correct formula/<i>korrekte substitusie in korrekte formule</i></li> <li>✓ simplify denominator/<i>vereenvoudig noemer</i></li> <li>✓ answer/<i>antwoord</i></li> </ul>
<p><b>ALTERNATIVE/ALTERNATIEWE</b></p> <p><math>a = \sqrt{3}</math> <b>AND/EN</b> <math>r = \frac{\sqrt{3}-1}{\sqrt{3}}</math></p> $S_{\infty} = \frac{\sqrt{3}}{1 - \frac{\sqrt{3}-1}{\sqrt{3}}} = \frac{\sqrt{3}}{\frac{\sqrt{3}-(\sqrt{3}-1)}{\sqrt{3}}} = \sqrt{3} \times \sqrt{3}$ $= 3$	<p>If the steps from substitution to answer are not shown clearly, award max 2/4/As al die stappe vanaf substitusie tot by finale antwoord nie duidelik gewys word nie, gee maksimum 2/4</p>

3.3	<p>Geometric sequence/<i>Meetkundige ry</i></p> $T_3 + T_4 + T_5 = 28$ $\therefore ar^2 + ar^3 + ar^4 = 28$ $ar^2(1 + r + r^2) = 28$ $T_6 + T_7 + T_8 = 224$ $\therefore ar^5 + ar^6 + ar^7 = 224$ $ar^5(1 + r + r^2) = 224$ <p>Then <math>\frac{ar^5(1 + r + r^2)}{ar^2(1 + r + r^2)} = \frac{224}{28}</math></p> $\therefore r^3 = 8$ $r = 2 \quad \therefore a = 1$ <p>First three terms/<i>Eerst drie terme</i> : 1; 2; 4</p>	<ul style="list-style-type: none"> <li>✓ formula for sum of the 3 terms/<i>formule vir die som van 3 terme</i></li> <li>✓ factors/<i>faktore</i></li> <li>✓ ratio/<i>verhouding</i></li> <li>✓ BOTH <math>r</math> and <math>a</math>/<i>BEIDE r en a</i></li> <li>✓ first THREE terms/<i>eerste DRIE terme</i></li> </ul>
		[13]

<b>QUESTION 4/VRAAG 4</b>		
4.1		
4.1.1	<p>Substitute/Vervang <math>P(2; 8)</math></p> $y = a(x - 2)^2 + 8$ <p>Substitute/vervang <math>(0; 0)</math></p> $0 = a(0 - 2)^2 + 8$ $a = -2$ $\therefore y = -2(x - 2)^2 + 8$ $= -2(x^2 - 4x + 4) + 8 = -2x^2 + 8x$	✓ substitute/vervang $P$ ✓ substitute/vervang $(0; 0)$ ✓ value of $a$ /waarde van $a$ ✓ simplify/vereenvoudig (4)
	<p><b>ALTERNATIVE/ALTERNATIEWE</b></p> $y = a(x - 0)(x - 4)$ <p>Substitute/vervang <math>(2; 8)</math></p> $8 = a(2 - 0)(2 - 4)$ $a = -2$ $\therefore y = -2x(x - 4) = -2x^2 + 8x$	✓ x-intercepts/x-afsnitte ✓ substitute $P$ /vervang $P$ ✓ value of $a$ /waarde van $a$ ✓ simplify/vereenvoudig (4)

4.1.2	B(4;0)  $2x + 4 = -2x^2 + 8x$  $x^2 - 3x + 2 = 0$  $(x-1)(x-2) = 0$  $\therefore A(1; 6)$	✓ coordinates B/ koördinate B  ✓ equating/stel gelyk  ✓ coordinates A/ koördinate A  (3)
4.1.3	$f'(x).g(x) \leq 0$  $\therefore x \in (-\infty; -2] \cup x \in [2; \infty)$ <b>OR/OF</b>  $y \leq -2$ or/of $y \geq 2$	✓ values/waardes ✓ notation/notasie  (2)
4.1.4	Turning point (1; 7)/Draaipunt (1; 7)  $y \leq 7$ <b>OR/OF</b> $y \in (-\infty; 7]$	✓ (1; 7) ✓ answer/antwoord <b>Answer only/slegs antwoord</b> 2/2  (2)
4.1.5	$f'(x) = -4x + 8$  $\therefore -4x + 8 = 2$ $x = \frac{3}{2}$	✓ derivative/afgeleide  ✓ 2 ✓ answer/antwoord  (3)
4.2		
4.2.1	$x = 2$ <b>AND/EN</b> $y = 1$	✓✓  (2)
4.2.2	$m = -1$ <b>AND/EN</b> (3; 1)  $y - 1 = -1(x - 3)$ <b>OR/OF</b> $1 = -1(3) + c$  $y = -x + 4$ $c = 4$ $\therefore y = -x + 4$	✓ $m = -1$  ✓ substitute (3; 1)  ✓ answer/antwoord  (3)
		[19]

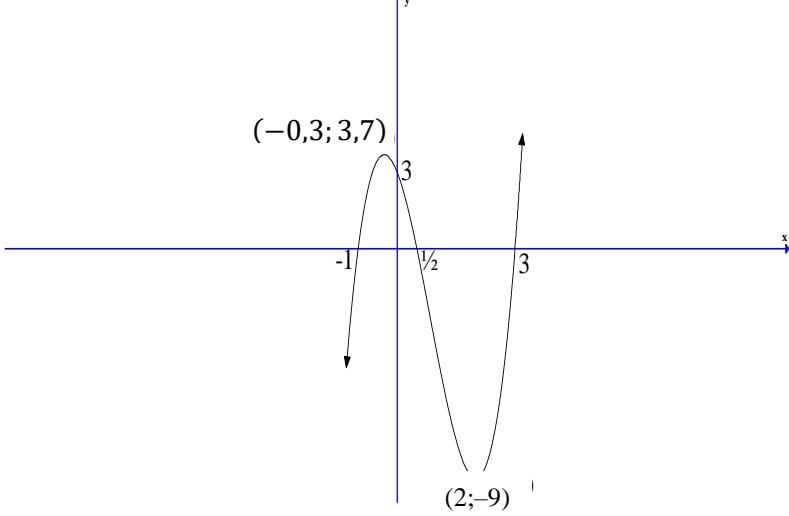
<b>QUESTION 5/VRAAG 5</b>		
5.1	$f(x) = 2^{-x}$ $\therefore g : x = 2^{-y}$ $-y = \log_2 x$ $y = -\log_2 x$ <b>OR/OF</b> $y = \log_2 x^{-1}$ <b>OR/OF</b> $y = \log_{\frac{1}{2}} x$	✓ interchange $x$ and $y$ /ruil $x$ en $y$ om ✓ answer/antwoord <b>Answer only full marks/slegs antwoord volpunte</b> (2)
5.2	Yes, $x$ values do not repeat/Ja, $x$ waardes herhaal nie <b>OR/OF</b> Yes, every $x$ value has unique $y$ value/Ja, elke $x$ waarde het 'n unieke $y$ waarde	✓ yes/ja ✓ valid reason/geldige rede (2)
5.3		$f$ : ✓ shape/vorm ✓ intercept/afsnit  $g$ : ✓ shape/vorm ✓ intercept/afsnit (4)
5.4	$\begin{aligned} h(x) &= 2^{-x+1} - 2 \\ &= 2^{-x} \cdot 2 - 2 \\ &= 2\left(\frac{1}{2}\right)^x - 2 \quad \text{OR/OF} \quad y = \frac{2}{2^x} - 2 \end{aligned}$	✓ correct translation indicated/korrekte translasie aangedui ✓ answer with POSITIVE exponent/antwoord met positiewe eksponent (2)
		<b>[10]</b>

<b>QUESTION 6/VRAAG 6</b>		
6.1	$A = P(1 - i)^n$ $\frac{3}{4}x = x(1 - 0,082)^n$ $\frac{3}{4} = (0,918)^n$ $\therefore n = \log_{0,918} 0,75$ $n = 3,36$ $\therefore 4 \text{ years/jaar}$	✓ values of A and P/waardes van A en P ✓ correct substitution in correct formula/korrekte substitusie in korrekte formule ✓ correct use of logs/korrekte gebruik van logs ✓ answer in years/antwoord in jare (4)
6.2	$F_v = \frac{x[(1+i)^n - 1]}{i}$ $58480 = \frac{x \left[ \left(1 + \frac{0,09}{12}\right)^{71} - 1 \right]}{\frac{0,09}{12}} \left(1 + \frac{0,09}{12}\right)^2$ $\therefore x = R 617,45$	✓ $\frac{0,09}{12}$ ✓ 71 ✓ correct substitution/korrekte substitusie ✓ $\left(1 + \frac{0,09}{12}\right)^2$ ✓ answer (5)

6.3		
6.3.1	$\left(1 + \frac{0,08}{4}\right)^4 = \left(1 + \frac{i}{12}\right)^{12}$ $\left(\sqrt[12]{1,08243216} - 1\right) \times 12 = i$ $i = 0,0794725..$ <p><math>\therefore 7,95\%</math> compounded monthly</p> $P_v = \frac{x \left[ 1 - (1+i)^{-n} \right]}{i}$ $1500000 = \frac{x \left[ 1 - \left(1 + \frac{0,0795}{12}\right)^{-240} \right]}{\frac{0,0795}{12}}$ $\therefore x = R 12499,96$	✓ correct substitution in correct formula/korrekte substitusie in korrekte formule ✓ 7,95% ✓ -240 ✓ $\frac{0,0795}{12}$ ✓ correct substitution into correct formula/korrekte substitusie in korrekte formule (5)
6.3.2	Outstanding balance/Uitstaande balans $= \frac{12499,96 \left[ 1 - \left(1 + \frac{0,0795}{12}\right)^{-96} \right]}{\frac{0,0795}{12}}$ $= R 885813,38$ <p><b>ALTERNATIVE/ALTERNATIEWE</b></p> Outstanding balance/Uitstaande balans $= 1500000 \left(1 + \frac{0,0795}{12}\right)^{144} - \frac{12499,96 \left[ \left(1 + \frac{0,0795}{12}\right)^{144} - 1 \right]}{\frac{0,0795}{12}}$ $= R 885814,82$	IF using $P_v$ method/Indien $P_v$ -metode ✓ -96 ✓ correct substitution/korrekte substitusie ✓ answer/antwoord <b>OR/OF</b> ✓ 144 ✓ correct substitution/korrekte substitusie ✓ answer/antwoord (3)

<b>QUESTION 7/VRAAG 7</b>		
	<b>-1 for notation only ONCE in this question</b> <b>-1 vir notasie slegs EEN keer in hierdie vraag</b>	
7.1	$f(x) = -x^2 - 2$ $f(x+h) = -(x+h)^2 - 2$ $= -x^2 - 2xh - h^2 - 2$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $= \lim_{h \rightarrow 0} \frac{-x^2 - 2xh - h^2 - 2 - (-x^2 - 2)}{h}$ $= \lim_{h \rightarrow 0} \frac{-2xh - h^2}{h}$ $= \lim_{h \rightarrow 0} \frac{h(-2x - h)}{h}$ $= -2x$	✓ $f(x + h)$ ✓ formula/formule ✓ correct substitution/korrekte substitusie ✓ factors/faktore ✓ answer/antwoord (5)
7.2		
7.2.1	$y = \frac{x}{3} + \sqrt[4]{x^3} - 5p^2$ $y = \frac{1}{3}x + x^{\frac{3}{4}} - 5p^2$ $\therefore \frac{dy}{dx} = \frac{1}{3} + \frac{3}{4}x^{-\frac{1}{4}}$	✓ $x^{\frac{3}{4}}$ ✓ $\frac{1}{3}$ ✓ $\frac{3}{4}x^{-\frac{1}{4}}$ (3) <b>-1 if -10p included/-1 as -10p ingesluit</b>
7.2.2	$D_x \left[ (2x^{-1} - \sqrt{5})^2 \right]$ $= D_x \left[ 4x^{-2} - 4\sqrt{5}x^{-1} + 5 \right]$ $= -8x^{-3} + 4\sqrt{5}x^{-2}$	✓ expand/brei uit ✓ $-8x^{-3}$ ✓ $4\sqrt{5}x^{-2}$ (3)
		<b>[11]</b>

<b>QUESTION 8/VRAAG 8</b>	
8.1	<p><math>y = 2x^3 + ax^2 + bx + 3</math></p> <p>Substitute <math>(2; -9)</math>/Vervang <math>(2; -9)</math></p> $-9 = 2(2)^3 + a(2)^2 + 2b + 3$ $-9 = 16 + 4a + 2b + 3$ $-28 = 4a + 2b$ $2a + b = -14 \quad \text{equation 1/vergelyking 1}$ $f'(x) = 6x^2 + 2ax + b$ $\therefore 0 = 6(2)^2 + 2a(2) + b$ $4a + b = -24 \quad \text{equation 2/vergelyking 2}$ <p>Equation 2 – equation 1/vergelyking 2 – vergelyking 1</p> $2a = -10$ $a = -5 \quad \therefore b = -24 - 4(-5) = -4$ <p><b>ALTERNATIVE/ALTERNATIEWE</b></p> <p>From equation 1/Uit vergelyking 1: <math>b = -14 - 2a</math> (6)</p> <p>Substitute in equation 2/Vervang in vergelyking 2:</p> $-24 = 4a - 14 - 2a$ $2a = -10$ $a = -5 \quad \therefore b = -24 - 4(-5) = -4$
8.2	<p><math>f(x) = 2x^3 - 5x^2 - 4x + 3</math></p> $f(-1) = 2(-1)^3 - 5(-1)^2 - 4(-1) + 3 = -2 - 5 + 4 + 3 = 0$ <p><math>\therefore (x + 1)</math> is a factor/is 'n faktor</p>

<p>8.3</p> $f(x) = (x+1)(2x^2 - 7x + 3)$ $= (x+1)(2x-1)(x-3)$ $\therefore x = -1; x = 3; x = \frac{1}{2}$ $f'(x) = 6x^2 - 10x - 4$ $0 = 3x^2 - 5x - 2$ $(3x+1)(x-2) = 0$ $\therefore (2; -9) \text{ AND/EN } \left(-\frac{1}{3}; \frac{100}{27}\right) \text{ turning points/draaipunte}$ 	<p><math>y = 3</math></p> <p><math>x = -1</math></p> <p><math>\checkmark \checkmark x = 3</math></p> <p><math>x = \frac{1}{2}</math></p> <p><math>\checkmark</math> shape/vorm</p> <p><math>\checkmark \left(-\frac{1}{3}; 3\frac{19}{27}\right)</math></p> <p><math>\checkmark (2; -9)</math></p> <p>(5)</p>
<p>8.4</p> $f''(x) = 12x - 10$ $0 = 6x - 5$ $x = \frac{5}{6}$ <p>Graph concave down when/grafiek konkaaf na onder as  <math>x &lt; \frac{5}{6}</math></p> <p><b>OR/OF</b></p> $x \in \left(-\infty; \frac{5}{6}\right)$	<p><math>\checkmark 12x - 10 = 0</math></p> <p><math>\checkmark</math> answer/antwoord</p> <p>(2)</p>
[15]	

<b>QUESTION 9/VRAAG 9</b>		
9.1	$V = l \times b \times h$ $1000 \text{ cm}^3 = 2x \text{ cm} \times x \text{ cm} \times h \text{ cm}$ $\therefore h = \frac{1000}{2x^2} = \frac{500}{x^2}$	✓ formula volume/formule volume ✓ substitution/ substitusie (2)
9.2	$SA = 2\left(x \times \frac{500}{x^2}\right) + 2\left(2x \times \frac{500}{x^2}\right) + 2(x \times 2x)$ $= \frac{1000}{x} + \frac{2000}{x} + 4x^2$ $= 3000x^{-1} + 4x^2$ $\therefore \frac{dA}{dx} = -3000x^{-2} + 8x$ $8x^3 = 3000$ $x^3 = 375$ $x = 7,21$ $\therefore l = 14,42 \text{ cm}; b = 7,21 \text{ cm}; h = 9,62 \text{ cm}$	✓ substitution/ substitusie ✓ answer/antwoord ✓ derivative = $0/\text{afgeleide} = 0$ ✓ value of $x/\text{waarde}$ van $x$ (4)
		<b>[6]</b>

<b>QUESTION 10/VRAAG 10</b>		
10.1	$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$ Let $P(B) = x$ $0,4 = 3x + x - 3x^2$ $3x^2 - 4x + 0,4 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{4 \pm \sqrt{(-4)^2 - 4(3)(0,4)}}{2(3)}$ $x = \frac{4 \pm \sqrt{11,2}}{6}$ $x = 1,22 \text{ n.a}$ $x = 0,11$ $\therefore P(B) = 0,11$	✓ $P(A \text{ and } B) = P(A) \times P(B)$ ✓ standard form/standaardvorm ✓ correct substitution/korrekte substitusie ✓ Answers with choice/antwoorde met keuse (4)

10.2	$P(\text{club and sleeps late}) = 0,6 \times 0,7 = 0,42$ $P(\text{cinema and sleeps late}) = 0,4 \times 0,4 = 0,16$ $\therefore P(\text{sleeps late}) = 0,42 + 0,16 = 0,58$	✓ 0,42 ✓ 0,16 ✓ 0,58 (3) [7]
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<b>QUESTION 11/VRAAG 11</b>		
11.1		
11.1.1	$5! = 120$	✓ 5! ✓ 120 (2)
11.1.2	$\frac{3! \times 2}{5!} = \frac{1}{10}$	✓ numerator /teller ✓ denominator/ noemer (2)
11.2		
11.2.1	$3 \times 7 \times 7 \times 3 = 441$	✓ 3 ✓ $7 \times 7$ ✓ 3 (3)
11.2.2	$\frac{3 \times 5 \times 4 \times 1}{7 \times 6 \times 5 \times 4} = \frac{1}{14}$	✓ 3 ✓ $5 \times 4$ ✓ 1 ✓ denominator/ noemer (4)
		[11]
	<b>TOTAL/TOTAAL: 150</b>	